CS 260: Foundations of Data Science

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HAVERFORD COLLEGE

Materials by Sara Mathieson

Admin

- **Lab 2** grades & feedback posted on Moodle

Outline for today

- Evaluation Metrics
  - Confusion matrices
  - Precision and recall
  - ROC curves
- Introduction to probability

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Goals of Evaluation

- Think about what metrics are important for the problem at hand

- Compare different methods or models on the same problem

- Common set of tools that other researchers/users can understand

Training and Testing

(high-level idea)

- **Separate** data into "**train**" and "**test**"
  - *n* = num training examples
  - *m* = num testing examples
- **Fit** (create) the model using **training data**
  - e.g. sea_ice_1979-2012.csv
- **Evaluate** the model using **testing data**
  - e.g. sea_ice_2013-2020.csv

Confusion Matrices

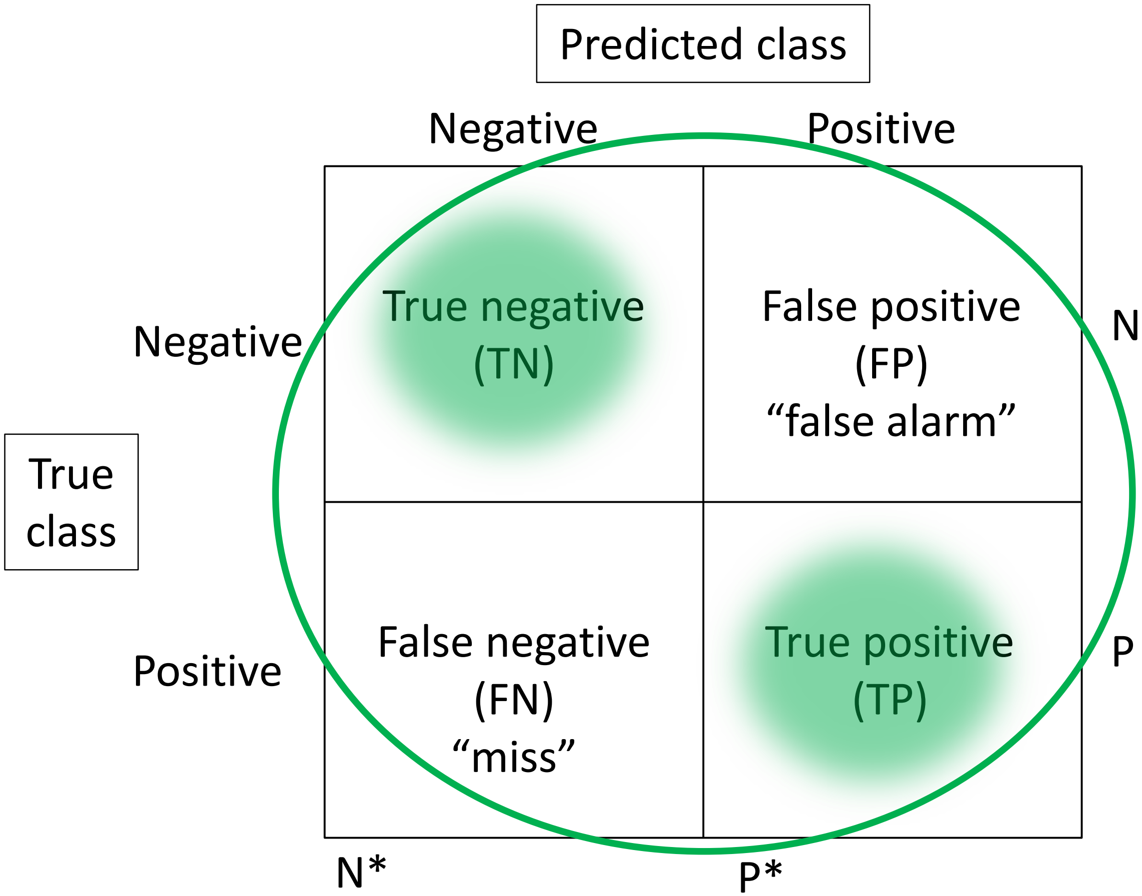
		Predicted class: Negative	Predicted class: Positive	
True class	Negative	True negative (TN)	False positive (FP) "false alarm"	N
	Positive	False negative (FN) "miss"	True positive (TP)	P
		N*	P*	

Error:

(FN+FP)/(TN+FP+FN+TP)

= (FN+FP)/(N+P)

Confusion Matrices



Accuracy = 1-Error:

(TN+TP)/(TN+FP+FN+TP)

= (TN+TP)/(N+P)

Confusion Matrices

True class	Predicted class: Negative	Predicted class: Positive	
Negative	True negative (TN)	False positive (FP) “false alarm”	N
Positive	False negative (FN) “miss”	True positive (TP)	P
	N*	P*	

Precision:

TP/(FP+TP) = TP/P*

Confusion Matrices

		Predicted class: Negative	Predicted class: Positive	
True class	Negative	True negative (TN)	False positive (FP) "false alarm"	N
	Positive	False negative (FN) "miss"	True positive (TP)	P
		N*	P*	

Recall
(True Positive Rate):

TP/(FN+TP) = TP/P

Confusion Matrices

Predicted class

True class	Negative	Positive	
Negative	True negative (TN)	False positive (FP) "false alarm"	N
Positive	False negative (FN) "miss"	True positive (TP)	P
	N*	P*	

False Positive Rate:

FP/(TN+FP) = FP/N

Modified from Jessica Wu

Precision and Recall

- Precision: of all the "flagged" examples, which ones are actually relevant (i.e. positive)?

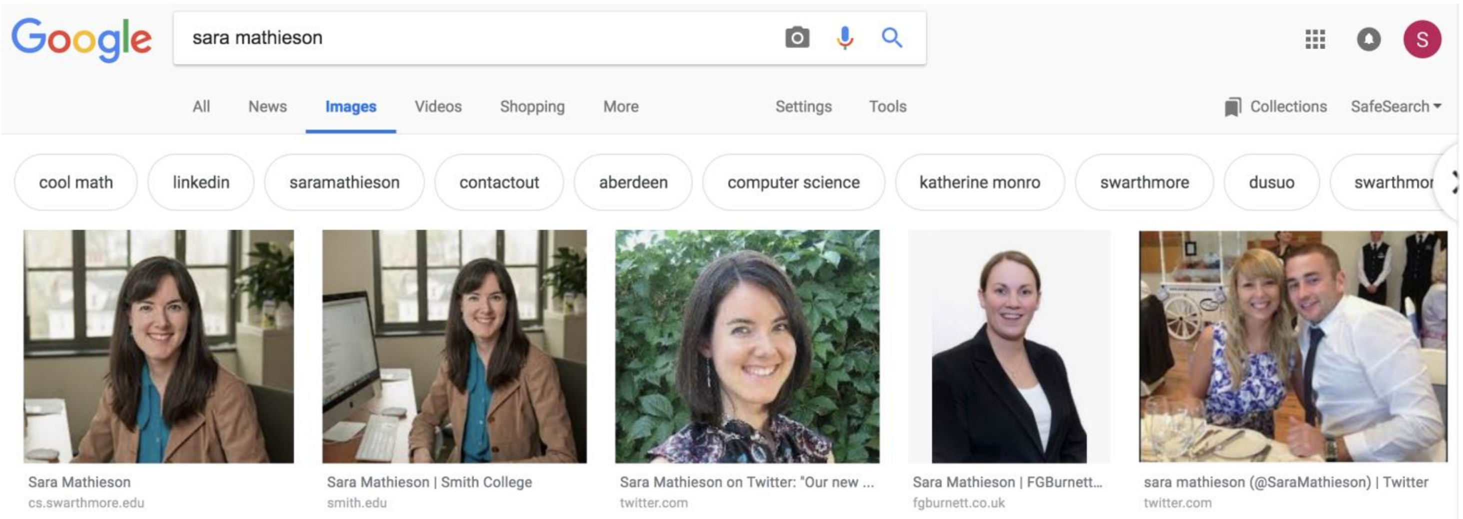
(Purity)

- Recall: of all the relevant results, which ones did I actually return?

(Completeness)

Modified from Ameet Soni

Precision and Recall

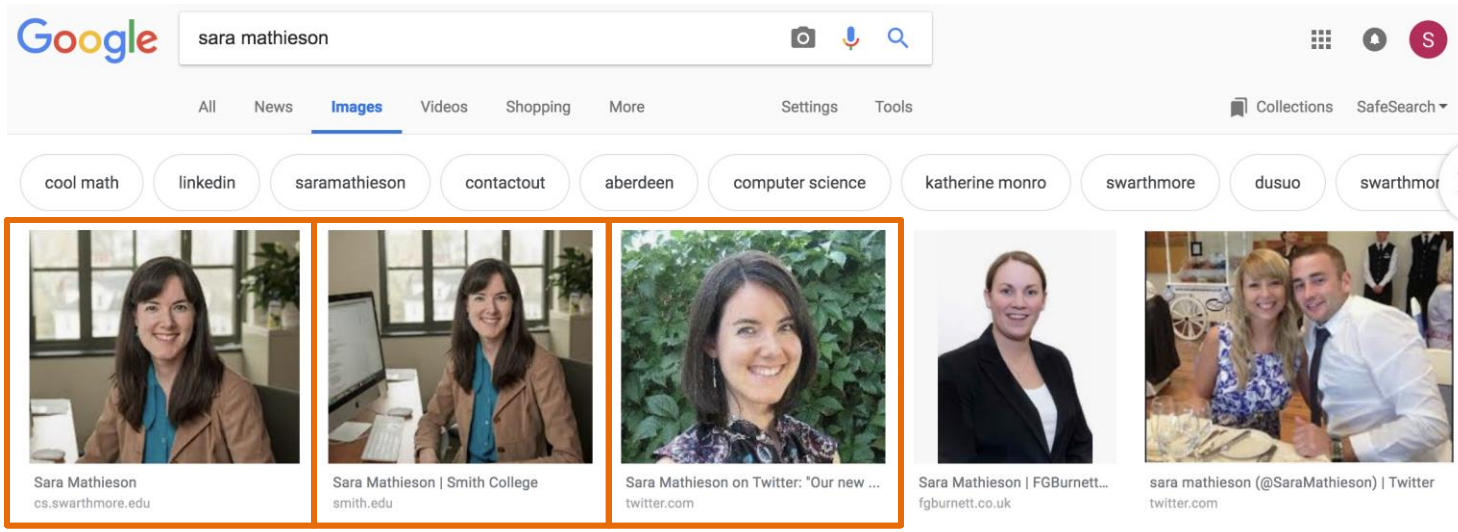


P=6 (number of images that are actually Sara)

- Precision?
- Recall?

Modified from Ameet Soni

Precision and Recall

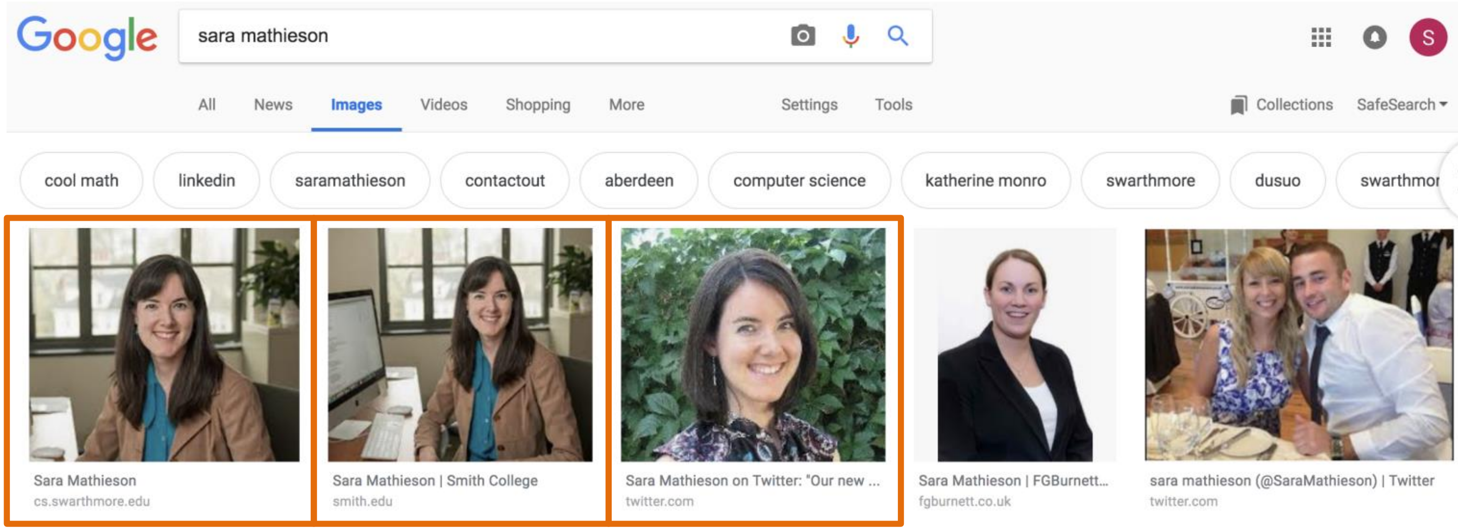


P=6 (number of images that are actually Sara)

- Precision = TP/(FP+TP) = 3/5
- Recall?

Modified from Ameet Soni

Precision and Recall

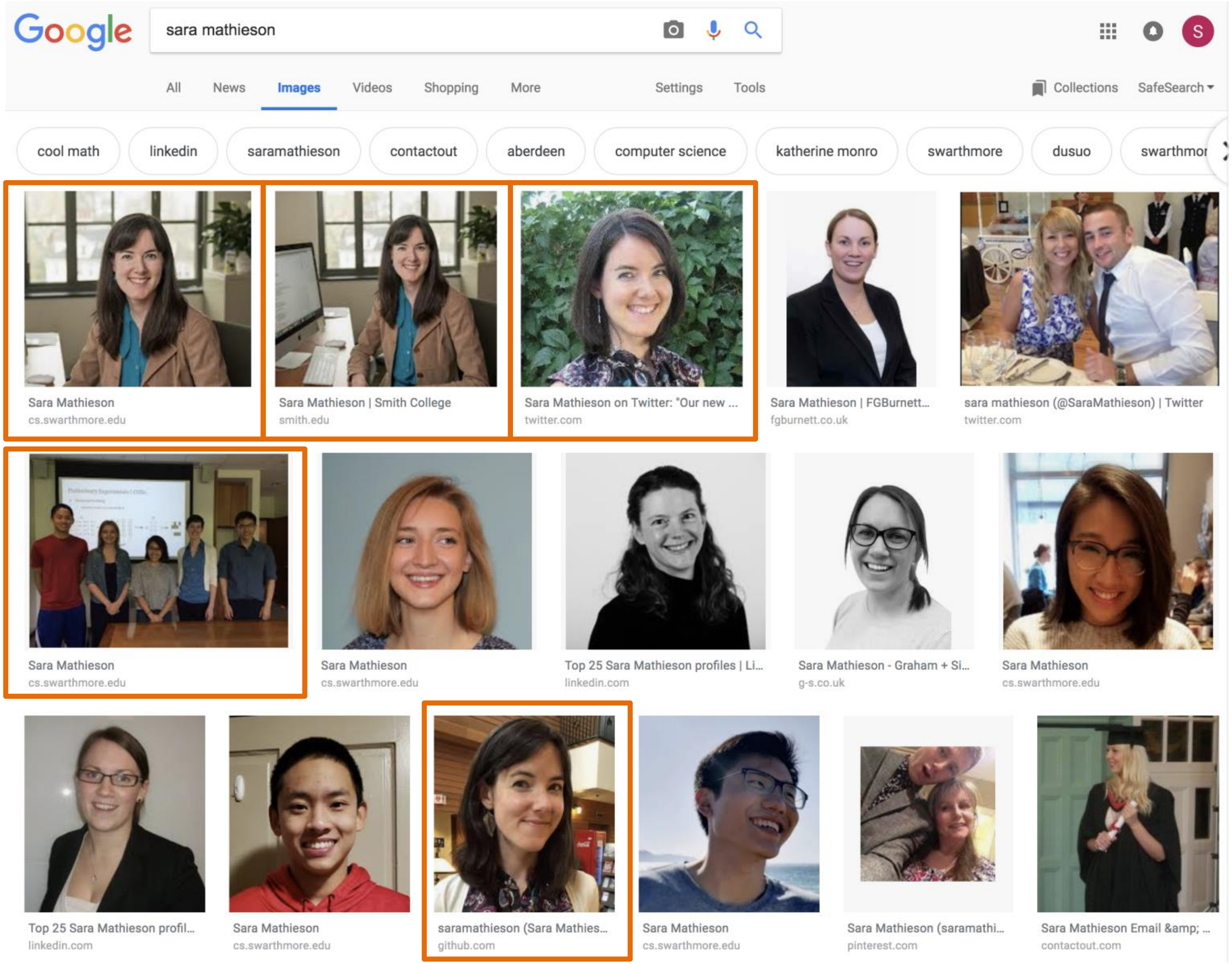


P=6 (number of images that are actually Sara)

- Precision = TP/(FP+TP) = 3/5
- Recall = TP/(FN+TP) = 3/6

Modified from Ameet Soni

Precision and Recall



P=6 (number of images that are actually Sara)

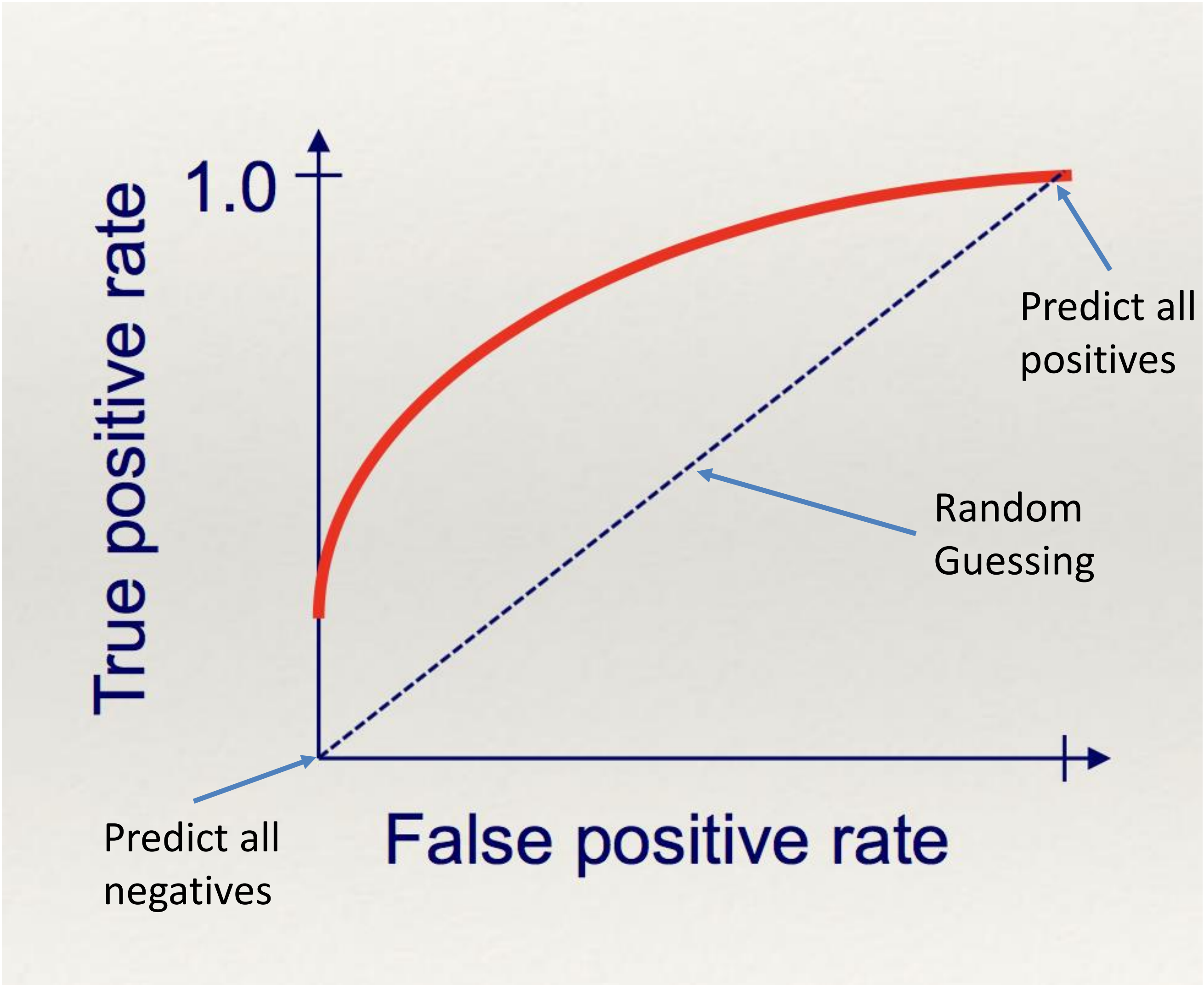
- Precision = 5/16
- Recall = 5/6

Modified from Ameet Soni

ROC curve (Receiver Operating Characteristic)

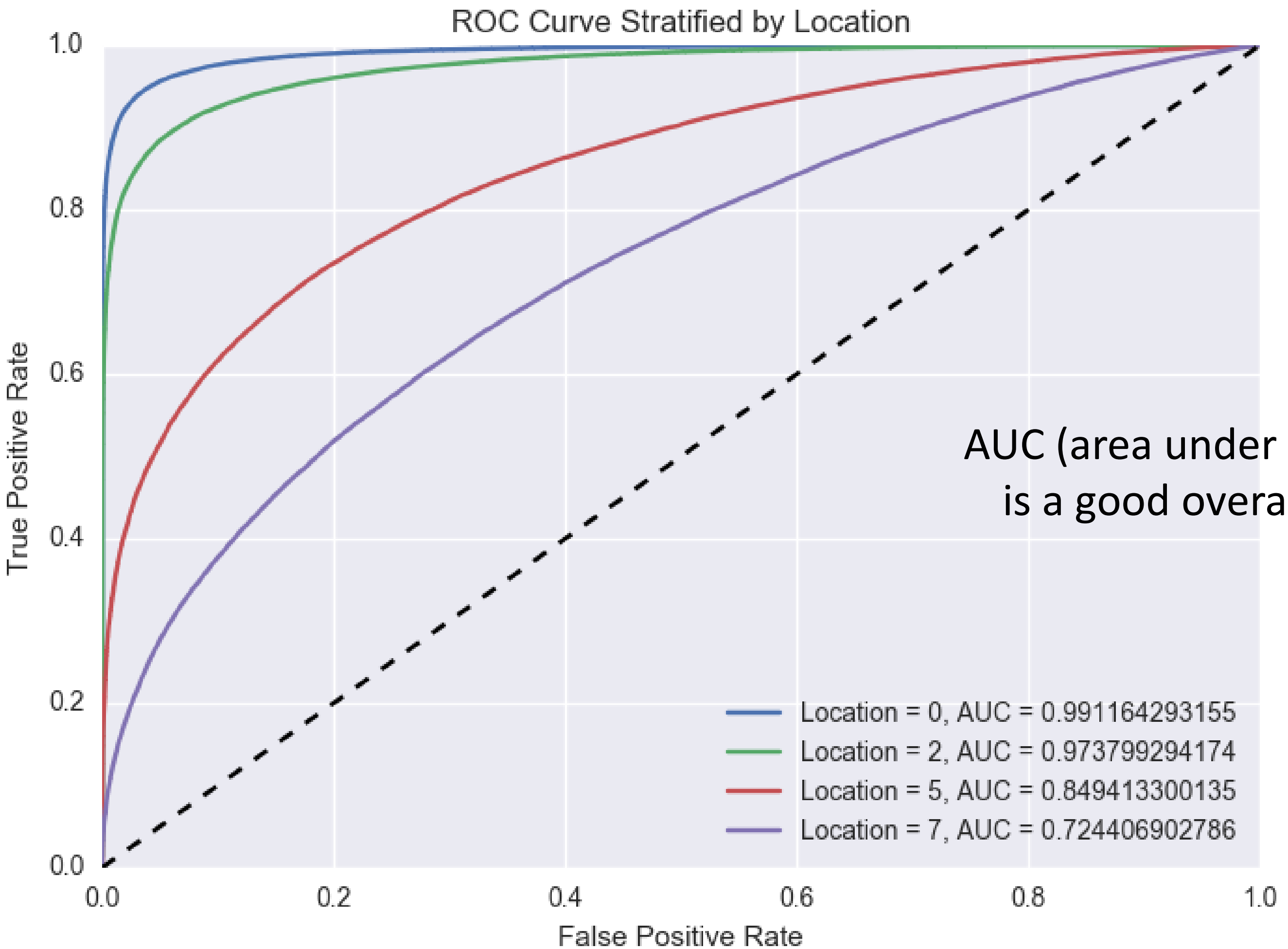
More history here!

https://en.wikipedia.org/wiki/Receiver_operating_characteristic



Modified from Ameet Soni

ROC curve example: comparing methods



AUC (area under the curve)
is a good overall metric

Example of a ROC curve
Chan, Perrone, Spence, Jenkins, Mathieson, Song

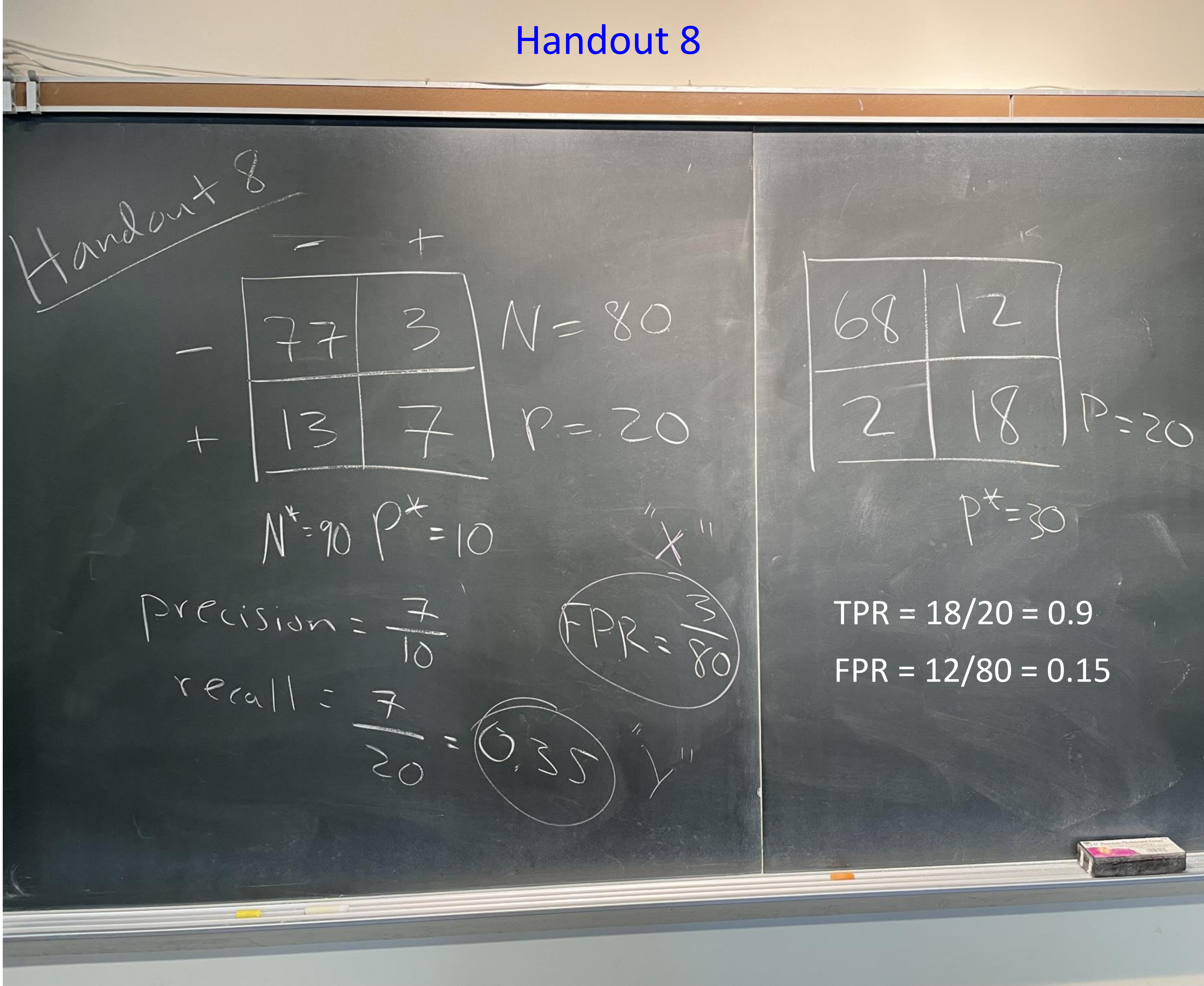
How to get a ROC curve for probabilistic methods?

- Usually we use 0.5 as a threshold for binary classification

- Vary the threshold! (i.e. choose 0, 0.1, 0.2,…)

  - $P(y=1 \mid x) >= 0.2$ => classify as 1 (positive)
  - $P(y=1 \mid x) < 0.2$ => classify as 0 (negative)

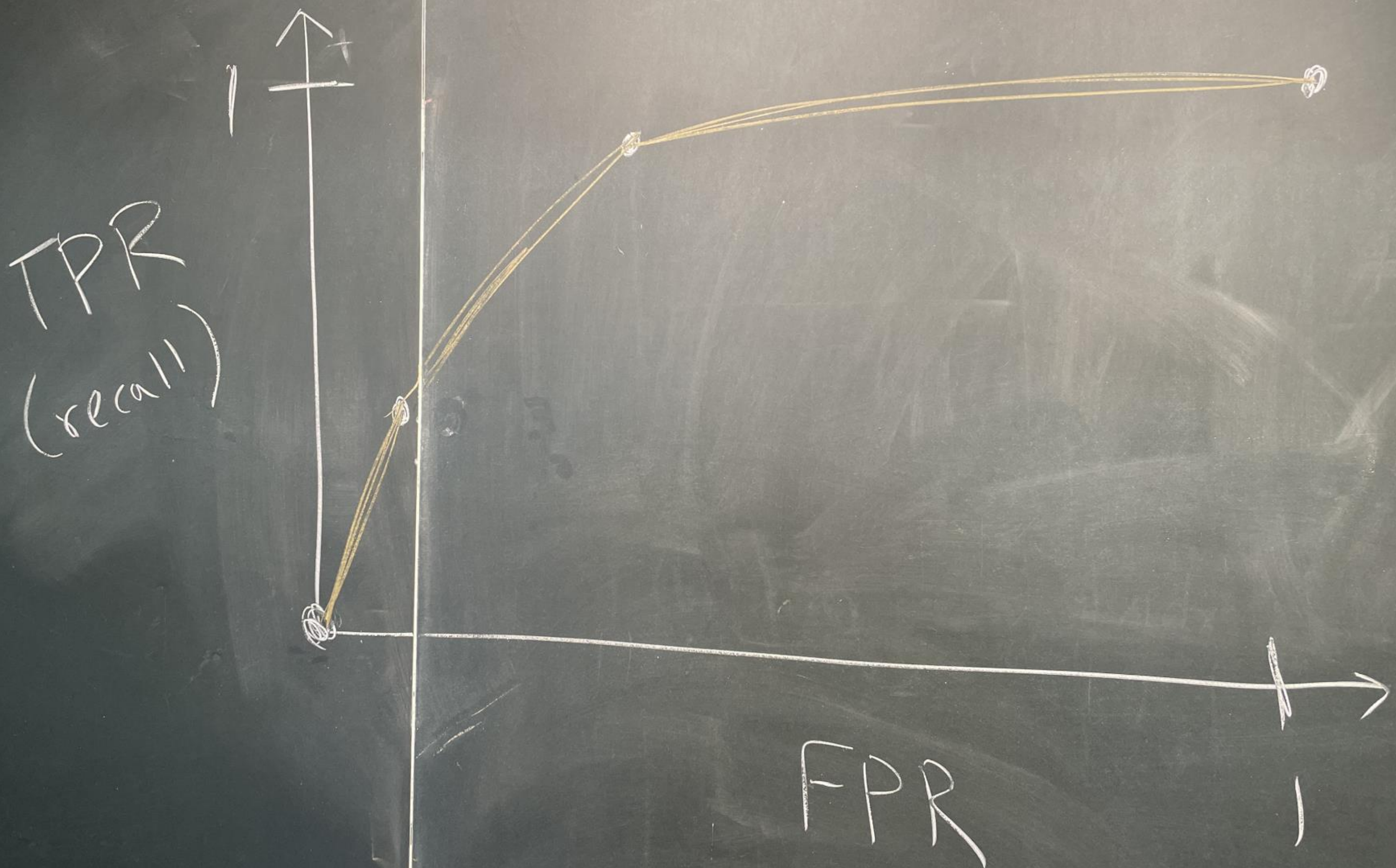
Handout 8



TPR = 18/20 = 0.9

FPR = 12/80 = 0.15

Handout 8



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- Introduction to probability

Intro to Probability

- The **probability** of an **event** e has a number of epistemological interpretations
- Assuming we have **data**, we can count the number of times e occurs in the dataset to estimate the probability of e, $P(e)$.

$$P(e) = \frac{\mathrm{count}(e)}{\mathrm{count}(\text{all events})}.$$

- If we put all events in a bag, shake it up, and choose one at random (called **sampling**), how likely are we to get e?

Materials by Alvin Grissom II

Intro to Probability

- Suppose we flip a fair coin
- What is the probability of heads, $P(e = H)$?

Materials by Alvin Grissom II

Intro to Probability

- Suppose we flip a fair coin
- What is the probability of heads, $P(e = H)$?
- We have "all" of two possibilities, $e \in \{H, T\}$.
- $P(e = H) = \frac{count(H)}{count(H)+count(T)}$

Materials by Alvin Grissom II

Intro to Probability

- Suppose we have a fair 6-sided die.
- What's the probability of getting "1"?

Materials by Alvin Grissom II

Intro to Probability

- Suppose we have a fair 6-sided die.
- What's the probability of getting "1"?

$$\frac{count(s)}{count(1) + count(2) + count(3) + \cdots + count(6)} = \frac{1}{1+1+1+1+1+1} = \frac{1}{6}$$